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# A short note on the equivalence between 'best proximity' points and 'fixed point' results

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## Abstract

In this short note, we notice that, unexpectedly, some existing fixed point results and recently announced best proximity point results are equivalent.

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**Keywords:** best proximity;  $h$ -orbitally complete; fixed point

## 1 Introduction and preliminaries

In 1973 Geraghty [1] introduced the class  $S$  of functions  $\beta : [0, \infty) \rightarrow [0, 1]$  satisfying the following condition:

$$\beta(t_n) \rightarrow 1 \quad \text{implies} \quad t_n \rightarrow 0. \quad (1)$$

The author defined contraction mappings via functions from this class and proved the following result.

**Theorem 1.1** (Geraghty [1]) *Let  $(X, d)$  be a complete metric space and  $T : X \rightarrow X$  be an operator. If  $T$  satisfies the following inequality:*

$$d(Tx, Ty) \leq \beta(d(x, y))d(x, y) \quad \text{for any } x, y \in X, \quad (2)$$

where  $\beta \in S$ , then  $T$  has a unique fixed point.

Theorem 1.1 was generalized in several ways, see e.g. [2–6]. Recently, Caballero *et al.* [2] introduced the following contraction.

**Definition 1.1** ([7]) *Let  $A, B$  be two nonempty subsets of a metric space  $(X, d)$ . A mapping  $T : A \rightarrow B$  is said to be a Geraghty-contraction if there exists  $\beta \in S$  such that*

$$d(Tx, Ty) \leq \beta(d(x, y))d(x, y) \quad \text{for any } x, y \in A. \quad (3)$$

For the sake of completeness, we recall some basic definitions and fundamental results.

Let  $(X, d)$  be a metric space and  $(A, B)$  a pair of nonempty subsets of  $X$ . We consider the following notations:

$$\begin{aligned} d(A, B) &:= \inf\{d(a, b) : a \in A, b \in B\}; \\ d(x, B) &:= \inf\{d(x, b) : b \in B\}; \\ A_0 &:= \{a \in A : d(a, b) = d(A, B) \text{ for some } b \in B\}; \\ B_0 &:= \{b \in B : d(a, b) = d(A, B) \text{ for some } a \in A\}. \end{aligned}$$

Through this paper,  $\mathbb{N}$  denotes the set of natural numbers.

In [8], Sadiq Basha introduced the following concept.

**Definition 1.2** We say that  $B$  is approximatively compact with respect to  $A$  if and only if every sequence  $\{y_n\} \subset B$  satisfying the condition that  $\lim_{n \rightarrow \infty} d(x, y_n) = d(x, B)$  for some  $x$  in  $A$ , has a convergent subsequence.

**Definition 1.3** A mapping  $g : A \rightarrow A$  is called an isometry if

$$d(gx, gy) = d(x, y), \quad \forall (x, y) \in A \times A.$$

**Definition 1.4** (see e.g. [9]) Given a mapping  $T : A \rightarrow B$  and an isometry  $g : A \rightarrow A$ , the mapping  $T$  is said to preserve the isometric distance with respect to  $g$  if and only if

$$d(T(gx), T(gy)) = d(Tx, Ty), \quad \forall (x, y) \in A \times A.$$

Denote by  $\Xi$  the set of functions  $\varphi : [0, \infty) \rightarrow [0, \infty)$  satisfying the following conditions:

- (I)  $\varphi$  is continuous and nondecreasing;
- (II)  $\varphi(0) = 0$ ;
- (III)  $\lim_{t \rightarrow \infty} \varphi(t) = \infty$ .

The following notions were introduced by Sadiq Basha [9].

**Definition 1.5** A mapping  $T : A \rightarrow B$  is said to be a generalized proximal contraction of the first kind if and only if

$$\left. \begin{aligned} d(u, Tx) = d(A, B) \\ d(v, Ty) = d(A, B) \end{aligned} \right\} \implies d(u, v) \leq d(x, y) - \varphi(d(x, y)),$$

where  $x, y, u, v \in A$  and  $\varphi \in \Xi$ .

**Definition 1.6** A mapping  $T : A \rightarrow B$  is said to be a generalized proximal contraction of the second kind if and only if

$$\left. \begin{aligned} d(u, Tx) = d(A, B) \\ d(v, Ty) = d(A, B) \end{aligned} \right\} \implies d(Tu, Tv) \leq d(Tx, Ty) - \varphi(d(Tx, Ty)),$$

where  $x, y, u, v \in A$  and  $\varphi \in \Xi$ .

Inspired by these definitions, Amini-Harandi [3] introduced the following definition.

Denote by  $\Psi$  the set of functions  $\psi : [0, \infty) \rightarrow [0, \infty)$  satisfying the following conditions:

- (I)  $\psi$  is continuous and nondecreasing;
- (II)  $\psi(0) = 0$ ;
- (III)  $t \leq \psi(t)$  for each  $t \geq 0$ .

**Definition 1.7** A mapping  $T : A \rightarrow B$  is said to be a generalized Geraghty proximal contraction of the first kind if and only if

$$\left. \begin{aligned} d(u, Tx) = d(A, B) \\ d(v, Ty) = d(A, B) \end{aligned} \right\} \implies \psi(d(u, v)) \leq \beta(d(x, y))\psi(d(x, y)),$$

where  $x, y, u, v \in A$  and  $\psi \in \Psi, \beta \in S$ .

**Definition 1.8** A mapping  $T : A \rightarrow B$  is said to be a generalized Geraghty proximal contraction of the second kind if and only if

$$\left. \begin{aligned} d(u, Tx) = d(A, B) \\ d(v, Ty) = d(A, B) \end{aligned} \right\} \implies d(Tu, Tv) \leq \beta(d(Tx, Ty))\psi(d(Tx, Ty)),$$

where  $x, y, u, v \in A$  and  $\psi \in \Psi, \beta \in S$ .

The main result in [3] is the following.

**Theorem 1.2** Let  $A$  and  $B$  be two nonempty closed subsets of a complete metric space  $(X, d)$  such that  $A_0 \neq \emptyset, B_0 \neq \emptyset$  and  $B$  is approximatively compact with respect to  $A$ . Suppose that the mappings  $g : A \rightarrow A$  and  $T : A \rightarrow B$  satisfy the following conditions:

- (i)  $T$  is a generalized Geraghty proximal contraction of the first kind;
- (ii)  $T(A_0) \subseteq B_0$ ;
- (iii)  $g$  is an isometry;
- (iv)  $A_0 \subseteq g(A_0)$ .

Then there exists a unique element  $x^* \in A$  such that

$$d(gx^*, Tx^*) = d(A, B).$$

Further, for any fixed element  $x_0 \in A_0$ , the iterative sequence  $\{x_n\} \subset A_0$ , defined by

$$d(gx_{n+1}, Tx_n) = d(A, B),$$

converges to  $x^*$ .

In this manuscript, we shall show that Theorem 1.2 is a particular case of existing fixed point theorems in the literature. Hence, the main result of [3] is not a real generalization.

## 2 Some useful results

Denote by  $\Phi$  the set of functions  $\phi : [0, \infty) \rightarrow [0, \infty)$  satisfying the following conditions:

- (I)  $\phi$  is continuous and nondecreasing;
- (II)  $\phi(t) = 0$  if and only if  $t = 0$ .

First we show that we get the more general form of the main result in [3] by replacing the class of distance functions  $\Psi$  by  $\Phi$  in Definition 1.7.

**Theorem 2.1** *Let  $A$  and  $B$  be two nonempty closed subsets of a complete metric space  $(X, d)$  such that  $A_0 \neq \emptyset, B_0 \neq \emptyset$ , and  $B$  is approximatively compact with respect to  $A$ . Suppose that the mappings  $g : A \rightarrow A$  and  $T : A \rightarrow B$  satisfy the following conditions:*

(i)

$$\left. \begin{aligned} d(u, Tx) = d(A, B) \\ d(v, Ty) = d(A, B) \end{aligned} \right\} \implies \psi(d(u, v)) \leq \beta(d(x, y))\psi(d(x, y)),$$

where  $x, y, u, v \in A$  and  $\psi \in \Phi, \beta \in \mathcal{S}$ .

- (ii)  $T(A_0) \subseteq B_0$ ;
- (iii)  $g$  is an isometry;
- (iv)  $A_0 \subseteq g(A_0)$ .

Then there exists a unique element  $x^* \in A$  such that

$$d(gx^*, Tx^*) = d(A, B).$$

Further, for any fixed element  $x_0 \in A_0$ , the iterative sequence  $\{x_n\} \subset A_0$ , defined by

$$d(gx_{n+1}, Tx_n) = d(A, B),$$

converges to  $x^*$ .

*Proof* By following the lines in the proof of Theorem 3.1 in the paper of Amini-Harandi [3], we conclude that

$$\lim_{n \rightarrow \infty} d(x_n, x_{n+1}) = 0. \tag{4}$$

It is sufficient to prove that  $\{x_n\}$  is a Cauchy sequence.

Suppose, on the contrary, that  $\{x_n\}$  is not a Cauchy sequence. Then there exists  $\varepsilon > 0$  for which we can find subsequences  $\{x_{m(k)}\}$  and  $\{x_{n(k)}\}$  of  $\{x_n\}$  such that  $n(k) > m(k) > k$  and

$$d(x_{m(k)}, x_{n(k)}) \geq \varepsilon. \tag{5}$$

Furthermore, we can choose  $n(k)$ , associated with  $m(k)$ , is the smallest integer which satisfies  $n(k) > m(k) > k$  and (5). Consequently, we have

$$d(x_{m(k)}, x_{n(k)-1}) < \varepsilon. \tag{6}$$

Due to Lemma 2.4, we conclude that

$$\lim_{k \rightarrow \infty} d(x_{m(k)}, x_{n(k)}) = \lim_{k \rightarrow \infty} d(x_{m(k)-1}, x_{n(k)-1}) = \varepsilon. \tag{7}$$

So, we obtain

$$\begin{aligned} \psi(d(x_{m(k)}, x_{n(k)})) &= \psi(d(Tx_{m(k-1)}, Tx_{n(k-1)})) \\ &\leq \beta(d(x_{m(k-1)}, x_{n(k-1)}))\psi(d(x_{m(k-1)}, x_{n(k-1)})) \\ &\leq \psi(d(x_{m(k-1)}, x_{n(k-1)})). \end{aligned} \tag{8}$$

Letting  $k \rightarrow \infty$  in the inequality above, we get

$$\psi(\varepsilon) \leq \beta(d(x_{m(k-1)}, x_{n(k-1)}))\psi(\varepsilon) \leq \psi(\varepsilon),$$

since  $\psi$  is continuous and (7) holds. Due to the property of  $\psi$ ,  $\psi(\varepsilon) > 0$ , we derive

$$\lim_{k \rightarrow \infty} \beta(d(x_{m(k-1)}, x_{n(k-1)})) = 1 \tag{9}$$

from the last inequality above. Since  $\beta \in S$ , we conclude that

$$\lim_{k \rightarrow \infty} d(x_{m(k-1)}, x_{n(k-1)}) = 0. \tag{10}$$

Due to (7) we get  $\varepsilon = 0$ , a contradiction. Hence,  $\{x_n\}$  is Cauchy.

The rest follows from the corresponding lines in the proof of Theorem 3.1 in the paper of Amini-Harandi [3].  $\square$

The following theorem is due to [10].

**Theorem 2.2** *Let  $(X, d)$  be a complete metric space and  $T : X \rightarrow X$  be an operator. If  $T$  satisfies the following inequality:*

$$\psi(d(Tx, Ty)) \leq \beta(d(x, y))\psi(d(x, y)) \quad \text{for any } x, y \in X, \tag{11}$$

where  $\beta \in S$  and  $\psi \in \Phi$ , then  $T$  has a unique fixed point.

The following concept was introduced by Ćirić in [11].

**Definition 2.1** *Let  $(X, d)$  be a metric space and  $f : X \rightarrow X$  be a self-mapping. We say that  $X$  is  $f$ -orbitally complete if and only if for any  $x \in X$ , if  $\{f^n x\}$  is a Cauchy sequence, then it converges to some element in  $X$ .*

It is evident that in Theorem 2.2, the notion of completeness of the metric space  $(X, d)$  can be replaced by the notion of  $f$ -orbitally completeness. Consequently, we derive the following fixed point result.

**Lemma 2.1** (cf. [7]) *Let  $(X, d)$  be a  $f$ -orbitally complete metric space, where  $f : X \rightarrow X$  is a self-mapping satisfying the following condition:*

$$\psi(d(fx, fy)) \leq \beta(d(x, y))\psi(d(x, y)), \quad \forall (x, y) \in X \times X, \tag{12}$$

where  $\psi \in \Psi$ ,  $\beta \in S$ . Then  $f$  has a unique fixed point  $x^* \in X$ . Moreover, for any  $x \in X$ , the sequence  $\{f^n x\}$  converges to  $x^*$ .

Regarding the analogy with the proof of Lemma 2.2 in [7].

**Lemma 2.2** (cf. [7]) *Let  $(A, B)$  be a pair of closed subsets of a metric space  $(X, d)$ . Suppose that the following conditions hold:*

- (i)  $A_0 \neq \emptyset$ ;
- (ii)  $B$  is *approximatively compact* with respect to  $A$ .

*Then the set  $A_0$  is closed.*

**Lemma 2.3** (cf. [7]) *Let  $A$  and  $B$  be nonempty subsets of a metric space  $(X, d)$  such that  $A_0 \neq \emptyset$ . Suppose that the mappings  $g : A \rightarrow A$  and  $T : A \rightarrow B$  satisfy the following conditions:*

- (i)  $T$  is a *generalized Geraghty-proximal contraction of the first kind*;
- (ii)  $T(A_0) \subseteq B_0$ ;
- (iii)  $g$  is an *isometry*;
- (iv)  $A_0 \subseteq g(A_0)$ .

*Then there exists a self-mapping  $f : A_0 \rightarrow A_0$  satisfying the condition:*

$$d(Tx, g(fx)) = d(A, B), \quad \forall x \in A_0. \tag{13}$$

Regarding the analogy with the proof of Lemma 2.4 in [7].

**Lemma 2.4** ([12]) *Let  $(X, d)$  be a metric space and let  $(x_n)$  be a sequence in  $X$  such that  $(d(x_{n+1}, x_n))$  is non-increasing and*

$$\lim_{n \rightarrow +\infty} d(x_{n+1}, x_n) = 0.$$

*If  $(x_n)$  is not a Cauchy sequence, then there exist  $\varepsilon > 0$  and two sequences  $(m_k)$  and  $(n_k)$  of positive integers such that  $m_k > n_k \geq k$  and the following four sequences tend to  $\varepsilon$  when  $k \rightarrow +\infty$ :*

$$(d(x_{m_k}, x_{n_k})), \quad (d(x_{n_k}, x_{m_{k+1}})), \quad (d(x_{m_k}, x_{n_{k+1}})), \quad (d(x_{m_{k+1}}, x_{n_{k+1}})).$$

### 3 Main results

**Theorem 3.1** *Theorem 2.1 is a consequence of Theorem 2.2.*

*Proof* Suppose that all the assumptions of Theorem 1.2 are satisfied. From Lemma 2.3, there exists a self-mapping  $f : A_0 \rightarrow A_0$  satisfying (13). Then, for all  $(x, y) \in A_0 \times A_0$ , we have

$$\begin{cases} d(g(fx), Tx) = d(A, B), \\ d(g(fy), Ty) = d(A, B). \end{cases}$$

Since  $T$  is a generalized Geraghty-proximal contraction of the first kind and  $g$  is an isometry, we obtain

$$\psi(d(fx, fy)) = \psi(d(g(fx), g(fy))) \leq \beta(d(x, y))\psi(d(x, y)),$$

for every pair  $(x, y) \in A_0 \times A_0$ . Thus  $f$  satisfies inequality (11).

Since  $(X, d)$  is complete,  $(A_0, d)$  is also complete. From Theorem 2.2, the self-mapping  $h : A_0 \rightarrow A_0$  has a unique fixed point  $x^* \in A_0$ .

Note that from (13), since  $T$  is a generalized Geraghty-proximal contraction of the first kind and  $g$  is an isometry, we have  $x^* \in A_0$  is a fixed point of  $f$  if and only if  $x^* \in A$  and  $d(gx^*, Tx^*) = d(A, B)$ . Then there exists a unique  $x^* \in A_0$  such that  $d(gx^*, Tx^*) = d(A, B)$ . Now, let  $a \in A_0$  be an arbitrary point. Consider a sequence  $\{a_n\} \subset A_0$  satisfying

$$d(ga_{n+1}, Ta_n), \quad \forall n \in \mathbb{N}.$$

Since  $T$  is a generalized Geraghty-proximal contraction of the first kind and  $g$  is an isometry, it follows from (13) that

$$a_{n+1} = fa_n, \quad \forall n \in \mathbb{N}.$$

From Lemma 2.1, we have

$$\lim_{n \rightarrow \infty} d(a_n, x^*) = 0.$$

This ends the proof. □

#### 4 Consequences

**Theorem 4.1** *Let  $A$  and  $B$  be two nonempty closed subsets of a complete metric space  $(X, d)$  such that  $A_0 \neq \emptyset$  and  $B_0 \neq \emptyset$ . Suppose that the mappings  $g : A \rightarrow A$  and  $T : A \rightarrow B$  satisfy the following conditions:*

- (i)  $T$  is a generalized Geraghty proximal contraction of the first and second kind,

$$\left. \begin{aligned} d(u, Tx) = d(A, B) \\ d(v, Ty) = d(A, B) \end{aligned} \right\} \implies \psi(d(u, v)) \leq \beta(d(x, y))\psi(d(x, y)),$$

$$\left. \begin{aligned} d(u, Tx) = d(A, B) \\ d(v, Ty) = d(A, B) \end{aligned} \right\} \implies d(Tu, Tv) \leq \beta(d(Tx, Ty))\psi(d(Tx, Ty)),$$

where  $x, y, u, v \in A$  and  $\psi \in \Phi, \beta \in S$ ;

- (ii)  $T(A_0) \subseteq B_0$ ;
- (iii)  $g$  is an isometry;
- (iv)  $A_0 \subseteq g(A_0)$ .

Then there exists a unique element  $x^* \in A$  such that

$$d(gx^*, Tx^*) = d(A, B).$$

Further, for any fixed element  $x_0 \in A_0$ , the iterative sequence  $\{x_n\} \subset A_0$ , defined by

$$d(gx_{n+1}, Tx_n) = d(A, B),$$

converges to  $x^*$ .

**Theorem 4.2** *Theorem 4.1 is a consequence of Lemma 2.1.*

*Proof* Suppose that all the assumptions of Theorem 4.1 are satisfied. From Lemma 2.3, there exists a self-mapping  $f : A_0 \rightarrow A_0$  satisfying (13). Then, for all  $(x, y) \in A_0 \times A_0$ , we have

$$\begin{cases} d(g(fx), Tx) = d(A, B), \\ d(g(fy), Ty) = d(A, B). \end{cases}$$

Since  $T$  is a generalized Geraghty-proximal contraction of the first kind and  $g$  is an isometry, we obtain

$$\psi(d(fx, fy)) = \psi(d(g(fx), g(fy))) \leq \beta(d(x, y))\psi(d(x, y)),$$

for every pair  $(x, y) \in A_0 \times A_0$ . Thus  $f$  satisfies inequality (11).

Now, we shall prove that  $(A_0, d)$  is  $f$ -orbitally complete. Indeed, let  $x_0 \in A_0$  and consider the sequence  $\{x_n\} \subset A_0$  defined by  $x_n = f^n x_0$  for all  $n \in \mathbb{N}$ . Suppose that  $\{x_n\}$  is a Cauchy sequence, we have to prove that  $\{x_n\}$  converges to some element in  $A_0$ . Since  $(X, d)$  is complete and  $A$  is closed, there exists some  $z \in A$  such that

$$\lim_{n \rightarrow \infty} d(x_n, z) = 0. \tag{14}$$

By the definition of  $f$ , for all  $n \in \mathbb{N}$ , we have

$$\begin{cases} d(g(fx_n), Tx_n) = d(A, B), \\ d(g(fx_{n+1}), Tx_{n+1}) = d(A, B), \end{cases}$$

which implies (since  $T$  is a generalized Geraghty-proximal contraction of the second kind) that

$$\begin{aligned} \psi(d(T(gx_{n+1}), T(gx_{n+2}))) &= \psi(d(T(gfx_n), T(gfx_{n+1}))) \\ &\leq \beta(d(Tx_n, Tx_{n+1}))\psi(d(Tx_n, Tx_{n+1})), \end{aligned}$$

for all  $n \in \mathbb{N}$ . Since  $T$  preserves the isometric distance with respect to  $g$ , we obtain

$$\psi(d(Tx_{n+1}, Tx_{n+2})) \leq \beta(d(Tx_n, Tx_{n+1}))\psi(d(Tx_n, Tx_{n+1})), \quad \forall n \in \mathbb{N}.$$

Following the same lines as the proof of Theorem 3.1 in [3], one can show that  $\{Tx_n\}$  is a Cauchy sequence in the complete metric space  $(X, d)$ . Since  $B$  is closed, there exists some  $b \in B$  such that

$$\lim_{n \rightarrow \infty} d(Tx_n, b) = 0. \tag{15}$$

Now, using (14), (15), and the definition of  $f$ , we get

$$d(A, B) = \lim_{n \rightarrow \infty} d(g(fx_n), Tx_n) = \lim_{n \rightarrow \infty} d(gx_{n+1}, Tx_n) = d(gz, b).$$

Note that since  $g$  is an isometry, it is continuous. Now, we have

$$d(A, B) = d(gz, b), \quad b \in B.$$



This implies that  $gz \in A_0$ . On the other hand, since  $A_0 \subseteq g(A_0)$  and  $g$  is an isometry, we obtain  $z \in A_0$ . Thus, we proved that  $A_0$  is  $f$ -orbitally complete. Now, applying Lemma 2.1, we find that  $f$  has a unique fixed point  $x^* \in A_0$ .

The rest follows from the lines of the proof of Theorem 3.1.  $\square$

#### Competing interests

The authors declare that they have no competing interests.

#### Authors' contributions

All authors contributed equally and significantly in writing this article. All authors read and approved the final manuscript.

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